

TRIG IDENTITIES:

→ **RECIPROCAL**

$\csc \theta = \frac{1}{\sin \theta}$ $\sec \theta = \frac{1}{\cos \theta}$

$\cot \theta = \frac{1}{\tan \theta}$

→ **QUOTIENT**

$\tan \theta = \frac{\sin \theta}{\cos \theta}$ $\cot \theta = \frac{\cos \theta}{\sin \theta}$

$\tan \theta = \frac{\sec \theta}{\csc \theta}$ $\cot \theta = \frac{\csc \theta}{\sec \theta}$

→ **PYTHAGOREAN**

$\sin^2 \theta + \cos^2 \theta = 1$

$1 + \cot^2 \theta = \csc^2 \theta$

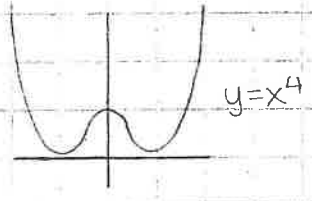
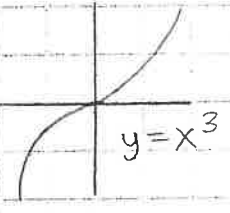
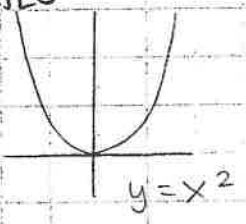
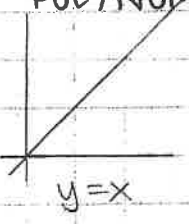
$\tan^2 \theta + 1 = \sec^2 \theta$

→ **DOUBLE ANGLE ARGUMENT**

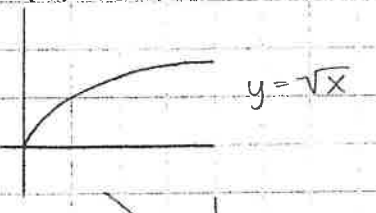
$\sin(2A) = 2 \sin A \cos A$

$\cos(2A) = \cos^2 A - \sin^2 A$

POLYNOMIALS



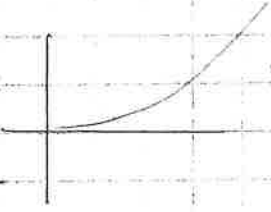
RADICALS



RATIONALS



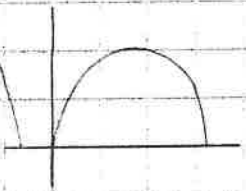
EXPONENTIAL



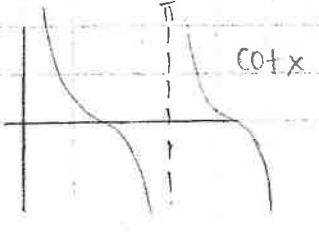
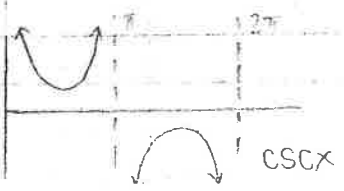
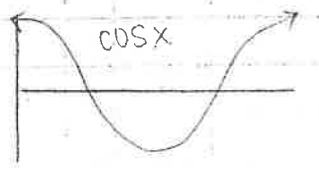
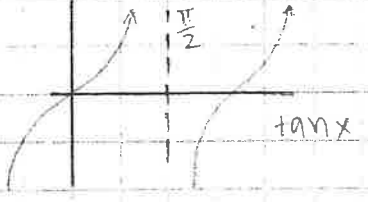
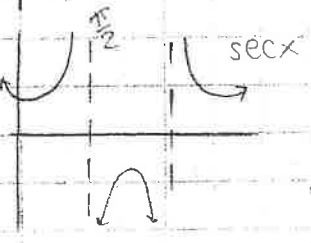
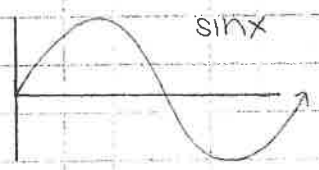
LOGARITHMIC

inverse
e

* usually limited ranges/ domains



TRIGONOMETRIC



RULES OF RADICALS: $\sqrt[n]{x} = x^{1/n}$, $\sqrt[n]{x^a} = x^{a/n}$

RULES OF EXPONENTS: $x^a x^b = x^{a+b}$, $(x^a)^b = x^{a \cdot b}$, $x^a / x^b = x^{a-b}$, $x^{-n} = \frac{1}{x^n}$

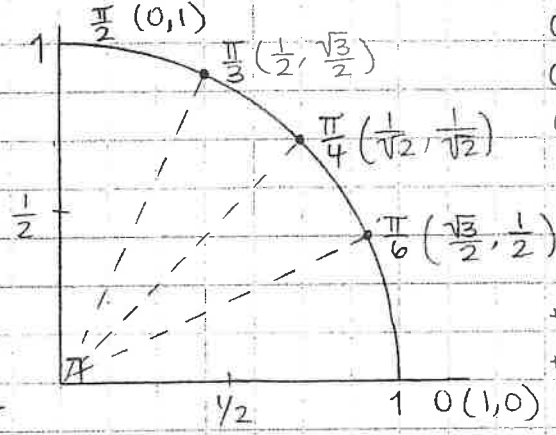
RULES OF LOGS: $\log_a x + \log_a y = \log_a (xy)$, $\log_a x - \log_a y = \log_a \frac{x}{y}$, $\log_a x^n = n \log_a x$

EXTRA

FACTS:

$\ln 1 = 0$
 $\ln e = 1$
 $\ln e^u = u$
 $e^{\ln u} = u$

THE UNIT CIRCLE:



KEY SPECIFIC VALUES:

$\cos(x) = 0 \rightarrow x = \frac{\pi}{2} \pm \pi n$

$\cos(x) = 1 \rightarrow x = 0 \pm 2\pi n$

$\cos(x) = -1 \rightarrow x = \pi \pm 2\pi n$

$\sin(x) = 0 \rightarrow x = 0 \pm \pi n$

$\sin(x) = 1 \rightarrow x = \frac{\pi}{2} \pm 2\pi n$

$\sin(x) = -1 \rightarrow x = -\frac{\pi}{2} \pm 2\pi n$

$\tan(x) = 0 \rightarrow x = 0 \pm \pi n$

$\tan(x) = 1 \rightarrow x = \frac{\pi}{4} \pm \pi n$

WHAT THE GRAPHS LOOK LIKE:

RANGES

- $y = \cos^{-1} x$ $0 \leq y \leq \pi$
- $y = \sin^{-1} x$ $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$
- $y = \tan^{-1} x$ $-\frac{\pi}{2} \leq y < \frac{\pi}{2}$
- $y = \cot^{-1} x$ $0 < y \leq \pi$
- $y = \sec^{-1} x$ $0 \leq y < \pi$
- $y = \csc^{-1} x$ $-\frac{\pi}{2} \leq y < \frac{\pi}{2}$

DERIVATIVE RULES:

$\frac{d}{dx} u = a \frac{du}{dx}$
 $\frac{d}{dx} u^n = nu^{n-1} \cdot \frac{du}{dx}$
 $\frac{d}{dx} (uv) = u \frac{dv}{dx} + v \frac{du}{dx}$
 $\frac{d}{dx} f(g(x)) = f'(g(x)) g'(x)$
 $\frac{d}{dx} (u+v) = \frac{du}{dx} + \frac{dv}{dx}$
 $\frac{d}{dx} a = 0$
 $\frac{d}{dx} \left(\frac{u}{v}\right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$
 $\frac{d}{dx} \sin u = \cos u \frac{du}{dx}$
 $\frac{d}{dx} \cos u = -\sin u \frac{du}{dx}$
 $\frac{d}{dx} \tan u = \sec^2 u \frac{du}{dx}$
 $\frac{d}{dx} \cot u = -\csc^2 u \frac{du}{dx}$
 $\frac{d}{dx} \sec u = \sec u \tan u \frac{du}{dx}$
 $\frac{d}{dx} \csc u = -\csc u \cot u \frac{du}{dx}$
 $\frac{d}{dx} a^u = a^u \ln a \frac{du}{dx}$
 $\frac{d}{dx} e^u = e^u \frac{du}{dx}$
 $\frac{d}{dx} \sin^{-1} u = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$
 $\frac{d}{dx} \cos^{-1} u = \frac{-1}{\sqrt{1-u^2}} \frac{du}{dx}$
 $\frac{d}{dx} \tan^{-1} u = \frac{1}{1+u^2} \frac{du}{dx}$

INTEGRAL RULES:

$\int u^n du = \frac{u^{n+1}}{n+1} + C, n \neq -1$
 $\int \frac{1}{u} du = \ln|u| + C \rightarrow e^C = k$
 $\int e^u du = e^u + C$
 $\int a^u du = \frac{a^u}{\ln a} + C, a > 0, a \neq 1$
 $\int \sin u du = -\cos u + C$
 $\int \cos u du = \sin u + C$
 $\int \sec^2 u du = \tan u + C$
 $\int \csc^2 u du = -\cot u + C$
 $\int \sec u du = \ln|\sec u + \tan u| + C$
 $\int \csc u du = \ln|\csc u - \cot u| + C$
 $\int \tan u du = \ln|\sec u| + C$
 $\int \cot u du = \ln|\sin u| + C$
 $\int \sin^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$
 $\int \cos^2 u du = \frac{1}{2}u + \frac{1}{4}\sin 2u + C$
 $\int \frac{du}{\sqrt{a^2-u^2}} = \sin^{-1}\left(\frac{u}{a}\right) + C$
 $\int \frac{du}{a^2+u^2} = \frac{1}{a} \tan^{-1}\left(\frac{u}{a}\right) + C$
 $\int \frac{du}{u\sqrt{u^2-a^2}} = \frac{1}{a} \sec^{-1}\left|\frac{u}{a}\right| + C$

FUNDAMENTAL THEOREM

① $\frac{d}{dx} \int_c^x f(t) dt = f(x)$
 $\frac{d}{dx} \int_c^u f(t) dt = f(u) \frac{du}{dx}$
 ② If $F'(x) = f(x)$ then
 $\int_a^b f(x) dx = F(b) - F(a)$

AVG VALUE:

$f_{avg} = \frac{1}{b-a} \int_a^b f(x) dx$

DISPLACEMENT:

$\int_a^b v(t) dt$

DISTANCE:

$\int_a^b |v(t)| dt$

MOTION:

$x(t) \rightarrow x'(t) = v(t) \rightarrow x''(t) = a(t)$

WASHER METHOD:

$V = \pi \int_a^b R^2 - r^2 dx$
 ↑ ↑
 outer inner

DISK METHOD:

$V = \pi \int_a^b R^2 dx$

LIMITS RULES:

$\lim_{x \rightarrow \infty} e^x = \infty, \lim_{x \rightarrow -\infty} e^x = 0$
 $\lim_{x \rightarrow -\infty} e^{-x} = \infty, \lim_{x \rightarrow \infty} e^{-x} = 0$

$\lim_{x \rightarrow -\infty} \tan^{-1} x = -\frac{\pi}{2}, \lim_{x \rightarrow \infty} \tan^{-1} x = \frac{\pi}{2}$

$\lim_{x \rightarrow -\infty} \cot^{-1} x = \pi, \lim_{x \rightarrow \infty} \cot^{-1} x = 0$

BOUNDARY RULES:

$\int_a^a f(x) dx = 0$
 $\int_a^b f(x) dx = -\int_b^a f(x) dx$
 $\int_a^b f(x) dx + \int_b^c f(x) dx = \int_a^c f(x) dx$
 If $f(x) \leq g(x)$ on $[a, b]$ then:
 $\int_a^b f(x) dx \leq \int_a^b g(x) dx$

MEAN VALUE THEOREM:

If a function f is continuous on $[a, b]$ and differentiable on (a, b) , then there is at least 1 number c such that $f'(c) = \frac{f(b) - f(a)}{b - a}$

ROLLE'S THEOREM:

If f is continuous on $[a, b]$ and differentiable on (a, b) and $f(a) = f(b)$, then there is at least 1 number c such that $f'(c) = 0$.
 like avg rate of change but not

EXTREME VALUE THEOREM: If f is continuous on closed $[a, b]$, then $f(x)$ has at least 1 max and 1 min between $f(a)$ and $f(b)$.

MODELS OF GROWTH + DECAY



$\frac{dy}{dt} = ky$
 exponential



$\frac{dy}{dt} = k(A - y)$
 simple bounded



$\frac{dy}{dt} = ky \left(1 - \frac{y}{A}\right)$
 logistic

INTERMEDIATE VALUE THEOREM:

Continuous, then $f(x)$ obtains every value between $f(a)$ and $f(b)$.