AP Calculus BC '17-18 Name_____
Anti Derivative Test

Score_____

1. Which of the following statements are true?

I. $\int \frac{1}{x\sqrt{x^2-16}}\,dx = \sec^{-1}\frac{x}{4}+c$

II. $\int \csc x\,dx = \ln\left|\csc x - \cot x\right| + c$

III. $\int \left(e^{6x}\sin e^{6x}\right)dx = \frac{1}{6}\cos e^{6x} + c$

a) I only b) II only c) III only

d) I and II only e) II and III only

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2. $\int x\sqrt{1-x^2}\,dx$

a) $\frac{\left(1-x^2\right)^{3/2}}{3}+c$ b) $-\left(1-x^2\right)^{3/2}+c$ c) $\frac{x^2\left(1-x^2\right)^{3/2}}{3}+c$

d) $\frac{-x^2\left(1-x^2\right)^{3/2}}{3}+c$ e) $\frac{-\left(1-x^2\right)^{3/2}}{3}+c$

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3. $\int \frac{1+\ln x}{x\ln x}\,dx =$

a) $\frac{1}{2}(1+\ln x)^2 + c$

b) $x+\ln x+c$

c) $\ln(\ln x)+c$

d) $\ln x+\ln(\ln x)+c$

e) $\frac{\ln x}{x+\ln x}+c$

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4. $\int (x^3)\sqrt{1-x^2}\,dx$

a) $\frac{x^4}{2}\cdot\frac{(1-x^2)^{3/2}}{3}+c$

b) $-\frac{1}{2}(1-x^2)^{1/2}-\frac{1}{3}(1-x^2)^{3/2}+c$

c) $-\frac{1}{3}(1-x^2)^{3/2}+\frac{1}{5}(1-x^2)^{5/2}+c$

d) $\frac{1}{3}(1-x^2)^{3/2}-\frac{1}{5}(1-x^2)^{5/2}+c$

e.) $\frac{-(1-x^2)^{3/2}}{3}+c$

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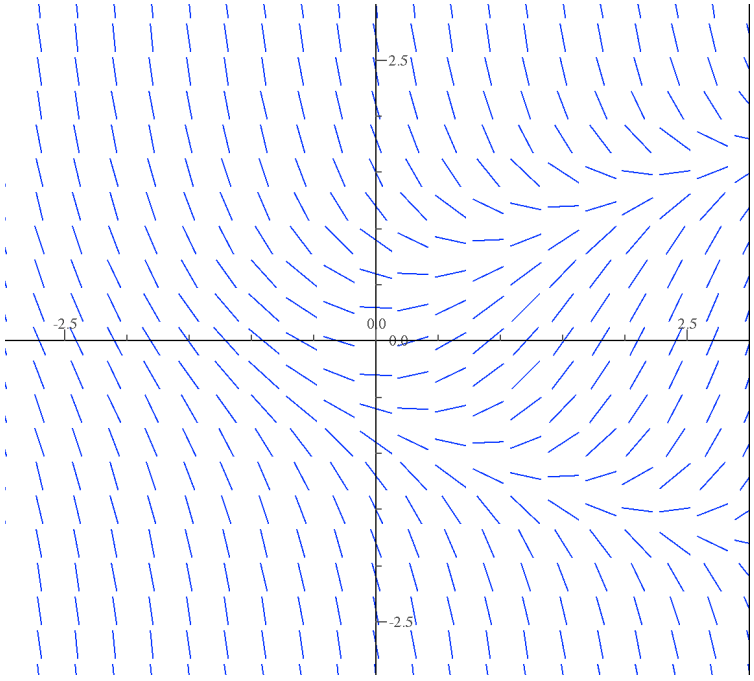
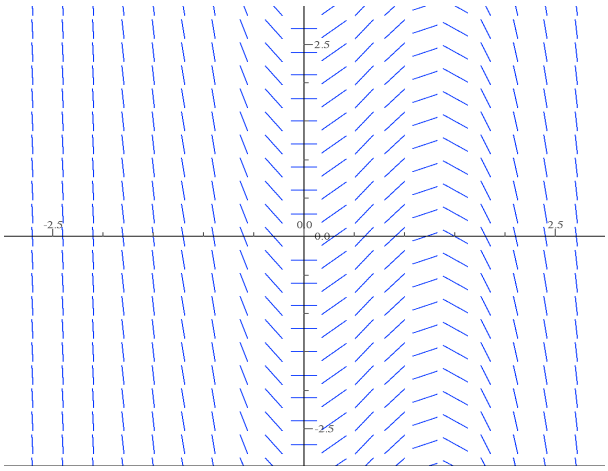
5. Which of the following differential equations corresponds to the slope field shown in the figure below?



a) $\frac{dy}{dx} = x - y^2$ b) $\frac{dy}{dx} = 1 - \frac{y}{x}$ c) $\frac{dy}{dx} = -y^3$

d) $\frac{dy}{dx} = x - \frac{1}{2}x^3$ e) $\frac{dy}{dx} = x + y$

6. Which of the following equations might be the solution to the slope field shown in the figure below?



a) $y = 4x - x^3$ b) $y = x^3 - 4x$ c) $y = 4x^4 - x^6$

d) $y = x^3 - 15x^5$ e) $y = \sec x$

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7. Identify is the first mistake (if any) in this process:

$$\frac{dy}{dx} = xy + x$$

Step 1: $\frac{1}{y+1}dy = xdx$

Step 2: $\ln|y+1| = x^2 + c$

Step 3: $|y+1| = e^{x^2} + c$

Step 4: $y = e^{x^2} + c$

a) Step 1 b) Step 2 c) Step 3

d) Step 4 e) There is no mistake.

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8. $\int \left(\frac{t^3 - 4t - 3}{5t^{2/3}} \right) dt$

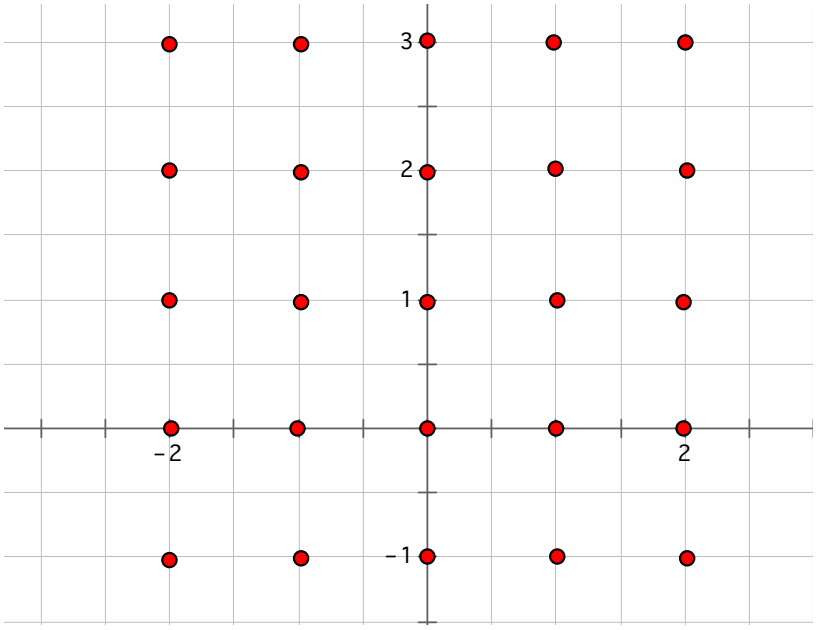
9. $\int \frac{x^5}{\left(x^3 - 1\right)^{3/2}} dx$

10. $\int\left(3x^8+\frac{\sec^2 x}{e^{\tan x}}-x^3\cot\left(x^4\right)\right)dx$

11. The acceleration of a particle is described by $a(t)=48t^2-18t+6$. Find the distance equation for *x(t)* if $v(1) = 1$ and $x(1) = 3$.

12. Given the differential equation, $\frac{dy}{dx} = \frac{y-2}{x+1}$

a. On the axis system provided, sketch the slope field for the $\frac{dy}{dx}$ at all points plotted on the graph.



b. If the solution curve passes through the point (0, 0), sketch the solution curve on the same set of axes as your slope field.

c. Find the equation for the solution curve of $\frac{dy}{dx}=(y-2)(x+1)$ given that $y(0)=5$