BC Calculus '17-18 Name _____
Dx Apps Test
No Calculator

1. If $g'(x) = 3xe^{2x} + 5$, then $g(x)$ has a point of inflection at:

a) $x = -1$ b) $x = 1/2$ c) $x = -1/2$

d) $x = 1$ e) Nowhere

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2. Given the functions $f(x)$ and $g(x)$ that are both continuous and differentiable, and that they have values given on the table below.

x	$f'(x)$	$f''(x)$	$g'(x)$	$g''(x)$
2	0	-2	8	0
4	8	0	0	3
8	0	-12	0	4

Then at $x = 8$, $g(x)$ has a:

a) Relative Maximum b) Relative Minimum

c) Point of Inflection d) Zero

e) None of these

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3. Suppose $f'(x)=\dfrac{(x+1)^3(x-4)^2}{(x^4+1)}$. Which of the following statements must be true?

I. The slope of the line tangent to $y=f(x)$ at $x=1$ is 36.

II. $f(x)$ is increasing on $x\in(1,\,4)$

III. $f(x)$ has a minimum at $x=-1$

a) I only b) II only c) III only d) I and II e) II and III only

ab) I and III only ac) I, II, and III ad) None of these

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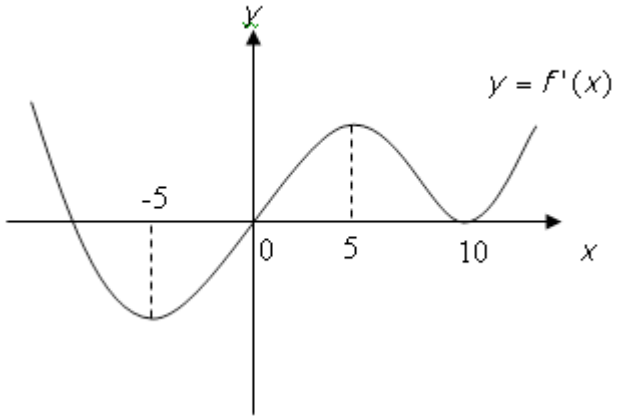
4. Below is the graph of $f'(x)$. For what value(s) of x does $f(x)$ have a minimum?



a) 0 only

b) 0 and 10

c) -5 and 5

d) -5 and 10

e) None of these

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5. A particle moves along the y-axis with position $s(t) = 15t^4 - 20t^3$. On what interval(s) is the particle slowing down?

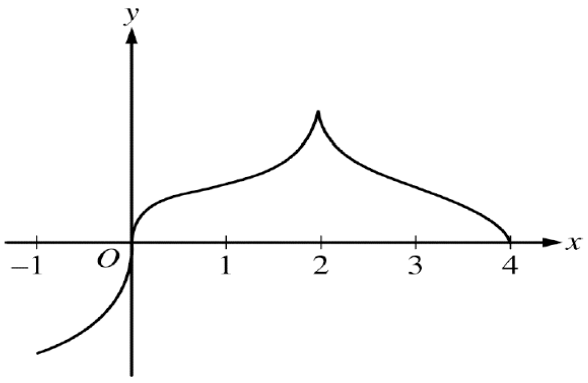
a) $t \in \left[\frac{2}{3}, \infty\right)$

b) $t \in (-\infty, 1]$

c) $t \in (-\infty, 0] \cup \left[\frac{2}{3}, 1\right]$

d) $t \in (-\infty, 0] \cup \left[1, \frac{2}{3}\right]$

e) $t \in (-\infty, 0]$



Graph of f'

6. The graph of f' is shown above. The line tangent to f' at $x = 0$ is vertical, and f' is not differentiable at $x = 2$. Which of the following statements is TRUE?

a.) f' does not exist at $x = 2$.

b) f is decreasing on the interval (2, 4)

c) The graph of f has a point of inflection at $x = 0$

d) The graph of f has a relative maximum at $x = 0$

e) The graph of f has a point of inflection at $x = 2$

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7. A particle's acceleration function is $a(t)=\sqrt[7]{7t-1}$, and its velocity is 0 at $t=0$. Which of these represents the particle's velocity function?

a) $v(t)=\frac{1}{8}\left[(7t-1)^{8/7}-1\right]$

b) $v(t)=\frac{1}{8}\left[7(5t-1)^{8/7}+1\right]$

c) $v(t)=\frac{1}{8}\left[7(8t-1)^{8/7}-1\right]$

d) $v(t)=\frac{1}{7}(7t-1)^{-6/7}$

e) $v(t)=\frac{1}{7}\left[(7t-1)^{-6/7}-1\right]$

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x	–2	0	3	5	6
$f'(x)$	3	1	4	7	5

8. Let f be a polynomial function with values $f'(x)$ at selected values of x given in the table above. Which of the following must be true for $-2 < x < 6$?

a) The graph of f is concave up.

b) The graph of f has at least two points of inflection.

c) f is increasing.

d) f has no critical points.

e) f has at least two relative extrema.

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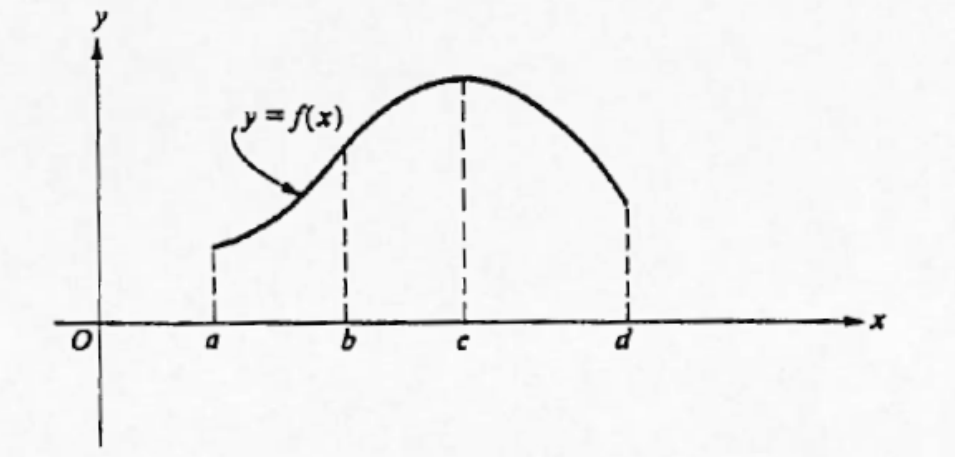
9. Find the absolute minimum value of $f(x)=2x^3+3x^2-12x+4$ on the closed interval $[0, 2]$.

a) -3 b) 0 c) 2 d) 4 e) 8



10. The graph $y=f(x)$ of is shown above. On which of the following intervals are $\frac{dy}{dx}>0$ and $\frac{d^2y}{dx^2}<0$

I. $a < x < b$ II. $b < x < c$ III. $c < x < d$

a) I only b) II only c) III only

d) I and II only e) None of these

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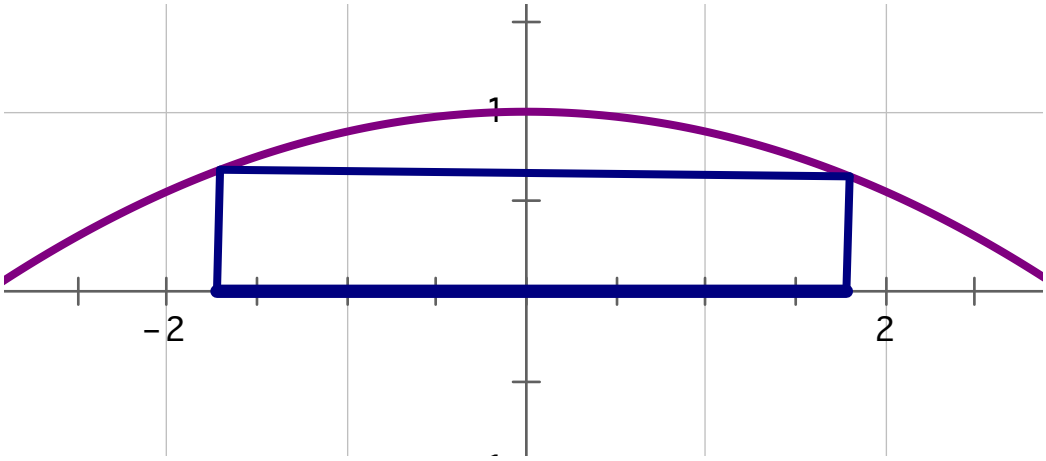
11. A rectangle with one side on the x-axis has its upper vertices on the graph of $y=1-\frac{x^2}{9}$, as shown in the figure below. What is the maximum area of the rectangle?



a) $\sqrt{3}$ b) $\frac{\sqrt{3}}{2}$ c) $\frac{2}{3}$ d) $\frac{4\sqrt{3}}{3}$ e) None of these

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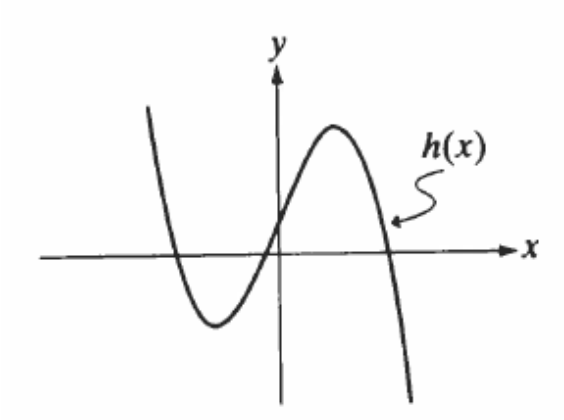
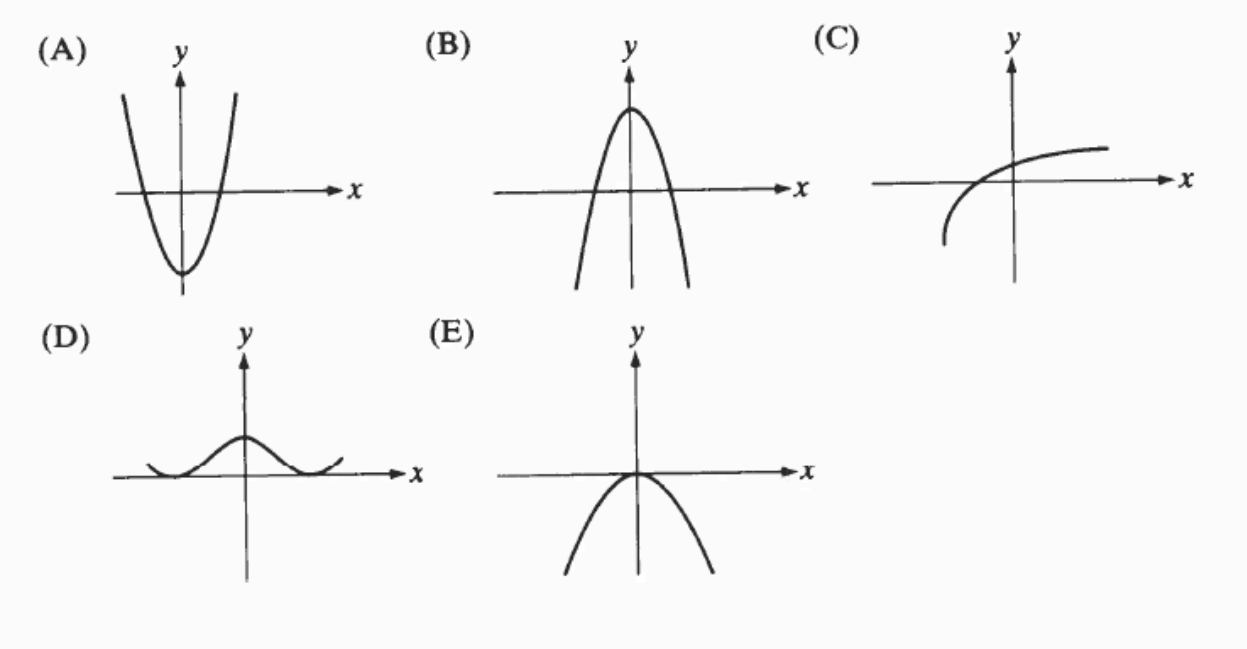
12. Suppose the function of h has the graph shown below. Which of the following could be the graph of $y = h'(x)$?





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Calculator allowed

Score_____

Directions: Show all work.

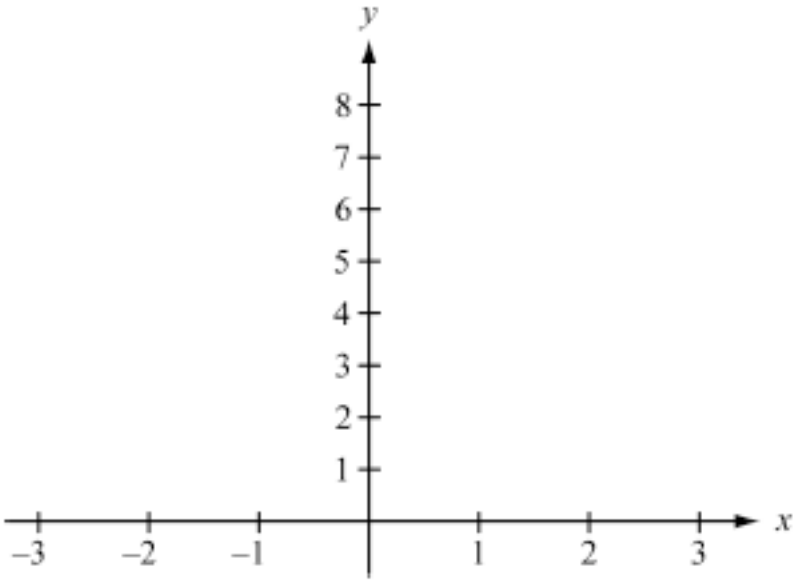
1. A function f is continuous on the interval $x \in [-3, 3]$ such that $f(-3) = 6$ and $f(3) = 1$. The functions f' and f'' have the properties given below.

x	$-3 \le x < -1$	$x = -1$	$-1 < x < 1$	$x = 1$	$1 < x \le 3$
$f'(x)$	Negative	0	Negative	DNE	Positive
$f''(x)$	Positive	0	Negative	DNE	Negative

(a) Find all the values of x for which f has a relative maximum or minimum on $x \in [-3, 3]$. Justify your answer.

(b) Find all the values of x for which f has a point of inflection on $x \in [-3, 3]$. Justify your answer.

(e) Sketch a graph of f.

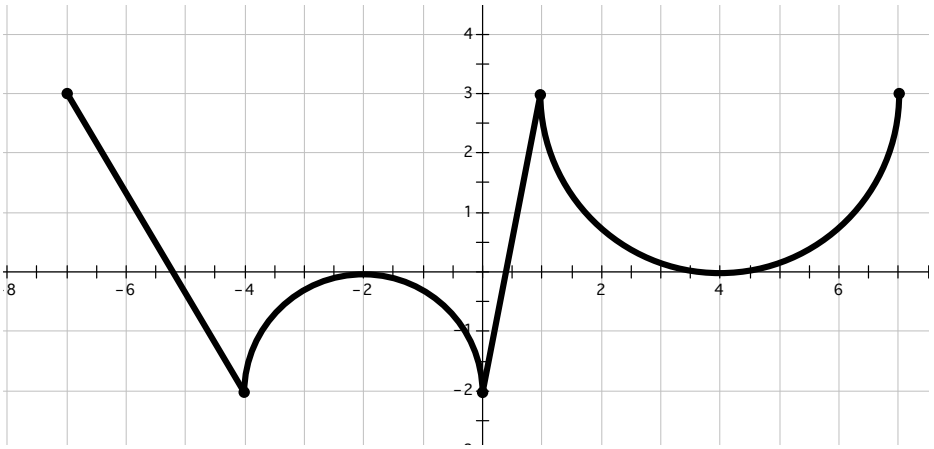


2. Consider the velocity equation $v(t)=\frac{3t}{t^2-4}$ on $x(2)=4$.

a) For what values is the particle moving right.

b) What is the acceleration at $t=3$? Show the derivative work.

c) Find the particular position equation.



3. The graph above is $f'(x)$ on $x \in [-7, 7]$.

a) Identify the *x*-value(s) of the relative maximums of $y = f(x)$? Justify your answer.

b) Identify the *x*-value(s) of the relative minimums of $y = f(x)$? Justify your answer.

c) Where are the points of inflection on $y = f(x)$? Justify your answer.