
INTEGRATION FORMULAS:

$$\int f(x) dx = F(x) + C, \text{ where } F'(x) = f(x)$$

$$\frac{d}{dx} \int_a^x f(t) dt = f(x) \quad \text{[First Fundamental Theorem]}$$

Remember the Chain Rule!!!: $\frac{d}{dx} \int_a^u f(t) dt = f(u) \cdot D_x u$

$$\int_a^b f(x) dx = F(b) - F(a), \text{ where } F'(x) = f(x) \quad \text{[Second Fundamental Theorem]}$$

$$\int u^n du = \frac{u^{n+1}}{n+1} + C, n \neq -1$$

$$\int \frac{du}{u} = \ln |u| + C$$

$$\int e^u du = e^u + C$$

$$\int a^u du = \frac{a^u}{\ln a} + C, (a > 0, a \neq 1)$$

$$\int \sin u du = -\cos u + C$$

$$\int \cos u du = \sin u + C$$

$$\int \sec^2 u du = \tan u + C$$

$$\int \csc^2 u du = -\cot u + C$$

$$\int \sec u \cdot \tan u du = \sec u + C$$

$$\int \csc u \cdot \cot u du = -\csc u + C$$

$$\int \sec u du = \ln | \sec u + \tan u | + C$$

$$\int \tan u du = \ln | \sec u | + C$$

$$\int \csc u du = \ln | \csc u - \cot u | + C$$

$$\int \cot u du = \ln | \sin u | + C$$

$$\int \sin^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$$

$$\int \cos^2 u du = \frac{1}{2}u + \frac{1}{4}\sin 2u + C$$

$$\int \frac{du}{\sqrt{a^2 - u^2}} = \sin^{-1}\left(\frac{u}{a}\right) + C$$

$$\int \frac{du}{a^2 + u^2} = \frac{1}{a} \cdot \tan^{-1}\left(\frac{u}{a}\right) + C$$

$$\int \frac{du}{u\sqrt{u^2 - a^2}} = \frac{1}{a} \cdot \sec^{-1}\left|\frac{u}{a}\right| + C$$

$$\int \frac{du}{u^2 - a^2} = \frac{1}{2a} \ln \left(\frac{u-a}{u+a} \right) + C$$

$$\int u dv = uv - \int v du$$