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Chapter 10 Test
CALCULATOR ALLOWED (20 min) Score $\qquad$
Round to 3 decimal places. Show all work.

1. If $f(x)=(x-1)\left(x^{2}+2\right)^{3}$, then $f^{\prime}(x)=$
a) $6 x\left(x^{2}+2\right)^{2}$
b) $\quad 6 x(x-1)\left(x^{2}+2\right)^{2}$
c) $\quad\left(x^{2}+2\right)^{2}\left(x^{2}+3 x-1\right)$
d) $\left(x^{2}+2\right)^{2}\left(7 x^{2}-6 x+2\right)$
e) $\quad-3(x-1)\left(x^{2}+2\right)^{2}$
2. If $h(t)=e^{2 t}(t+1)$, then $h^{\prime}(0)=$
a) 0
b) 1
c) 2
d) 3
e) 4
3. A particle is moving along the $x$-axis in such a way that its velocity at time $t>0$ is given by $v(t)=\frac{\ln t}{t}$. At what value of $t$ does $v$ attain its maximum?
(a) 1
(b) $e^{1 / 2}$
(c) $e$
(d) $e^{3 / 2}$
(e) There is no maximum value of $v$.
4. Let $f$ be a differentiable function with $f(4)=3$ and $f^{\prime}(4)=-2$, and let $g$ be a function defined by $g(x)=x f(x)$. Which of the following is an equation of the line tangent to the graph of $g$ at the point where $x=3$ ?
a) $y-12=-2(x-4)$
b) $y-12=\frac{1}{2}(x-4)$
c) $y-12=-5(x-4)$
d) $y-3=\frac{1}{5}(x-4)$
e) $y-12=\frac{1}{5}(x-4)$
5. $\lim _{x \rightarrow \infty} \frac{x^{2}}{e^{x}}=$
a) 0
b) $\quad \infty$
c) $-\infty$
d) 1
e) $e^{x}$


Graph of $f$


Graph of $g$
6. The graphs of the differentiable functions $f(x)$ and $g(x)$ are shown above. If $P(x)=f(x) g(x)$, which of the following will be true about $P^{\prime} ?$
a) $\quad P^{\prime}(2)<0$
b) $\quad P^{\prime}(2)>0$
c) $\quad P^{\prime}(0)>0$
d) $\quad P^{\prime}(0)<0$
e) $\quad P^{\prime}(0)=0$
7. Given the functions $f(x)$ and $g(x)$ that are both continuous and differentiable, and that have values given on the table below, find $h^{\prime}(4)$, given that $h(x)=g(x) \cdot f(x)$.

| $x$ | $f(x)$ | $f^{\prime}(x)$ | $g(x)$ | $g^{\prime}(x)$ |
| :---: | :---: | :---: | :---: | :---: |
| 2 | 4 | -2 | 8 | 1 |
| 4 | 10 | 8 | 4 | 3 |
| 8 | 6 | -12 | 2 | 4 |

a)
-12
b) 24
c) 0
d) -48
e) 62
8. Find the end behavior, if any, for $g(x)=e^{-2 x} \sqrt{x+1}$.
a) Left end none; $y=0$ on the right
b) Left end down; $y=0$ on the right
c) Left end $y=0$; right end up
d) Left end $y=0$; right end none
e) $y=0$ on the left and right
9. Which of the following is the equation of this graph?

a) $y=\ln \left(\left(x^{2}+9\right)(x-1)\right)$
b) $\quad y=\ln \left(\left(x^{2}-9\right)(x+1)\right)$
c) $y=\ln \left(\left(9-x^{2}\right)(x+1)\right)$
d) $y=\ln \left(\left(x^{2}-9\right)(x-1)\right)$

PreCalculus ACC '22-23 Name:
Chapter 10 Test - Form A
CALCULATOR ALLOWED
Score $\qquad$
Round to 3 decimal places. Show all work.

1. Find domain and $x$ - intercepts of $y=\left(x^{2}-8\right) e^{-\frac{1}{2} x}$.
2. Find the extreme points of $y=\left(x^{2}-8\right) e^{-\frac{1}{2} x}$. Show the algebraic work to support the critical values.
3. Find domain and $x$ - intercepts of $y=(x+1) \sqrt{9-x^{2}}$.
4. Find the extreme points of $y=(x+1) \sqrt{9-x^{2}}$. Show the algebraic work to support the critical values.
5. Find domain, VAs, and $x$ - intercepts of $f(x)=\ln \left(x^{3}-9 x\right)$ on $x \in[-4,5]$.
6. Find the extreme points of $f(x)=\ln \left(x^{3}-9 x\right)$ on $x \in[-4,5]$. Show the algebraic work to support the critical values.

## DO TWO OF THE FOLLOWING THREE SKETCHING PROBLEMS

7. Find the traits and sketch $y=\left(x^{2}-8\right) e^{-\frac{1}{2} x}$.

Domain:
$x$ - intercepts:

Extreme Points:

End Behavior (Left):
End Behavior (Right):
8. Find the traits and sketch of $f(x)=\ln \left(x^{3}-9 x\right)$ on $x \in[-4,5]$.

Domain:
$x$ - intercepts:

VAs:

End Behavior (Left):

Range:
$y$ - intercept:

Extreme Points:

End Behavior (Right):
9. Find the traits and sketch of $y=(x+1) \sqrt{9-x^{2}}$.

Domain:
VAs:

Extreme Points:

End Behavior (Left):

Range:
$y$ - intercept:

End Behavior (Right):

