

PreCalculus '13-14
Dr. Quattrin
Trig Basics
CALCULATOR ALLOWED
Round to 3 decimal places.

Name: Solution Key

Score _____

Round to 3 decimal places. Show all work.

1. $\sin\left(\cos^{-1}\frac{3}{4}\right) =$

a. 0.438

b. 0.661

c. 0.821

d. 1.3238

e. 1.528

2. The magnitude of $\vec{v} = 7\vec{i} - \sqrt{6}\vec{j}$ is

$$|\vec{v}| = \sqrt{7^2 + 6} = \sqrt{49 + 6}$$

a. $\sqrt{55}$

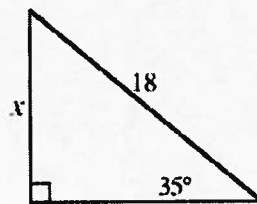
b. 1

c. 13

d. 85

~~e.~~ $\sqrt{85}$

3. In the triangle shown, which of the following best approximates x ?



$$\sin 35^\circ = \frac{x}{18}$$

a. 10.32

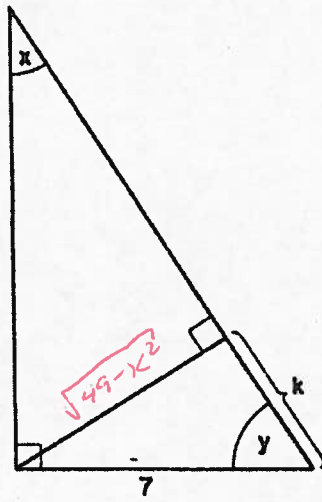
b. 25.71

c. 12.60

d. 14.74

e. none of these

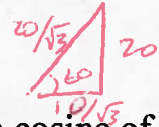
4. In the figure below, $\tan y =$



- a. $\frac{7}{k}$ b. $\frac{k}{7}$ c. $\frac{7-k}{7}$ d. $\frac{\sqrt{49-k^2}}{7}$ e. $\frac{\sqrt{49-k^2}}{k}$

5. An incline makes an angle of 60° with level ground. How many feet up the incline must one go in order to rise 20 feet above the ground?

- a. 10 b. $10\sqrt{3}$ c. $\frac{20}{\sqrt{3}}$ d. 40 e. $40\sqrt{3}$



6. What is the measure of an angle whose sine is twice the cosine of 60° ?

- a. 30° b. 60° c. 90°
 d. 120° e. No such angle

$$\begin{aligned} \cos 60 &= \frac{1}{2} \\ 2 \cos 60 &= 1 \\ \sin \theta &= 1 \\ \theta &= 90 \end{aligned}$$

PreCalculus 2013-14
 Trig Basics Practice Test
 Part II: CALCULATOR ALLOWED

Name SOLUTION KEY

Score _____

1. $(-3, 5)$ is on the terminal side of A. Find the six exact trig values:

$$r = \sqrt{34}$$

$$\sin A = \frac{5}{\sqrt{34}} \quad \cos A = \frac{-3}{\sqrt{34}}$$

$$\tan A = \frac{-5}{3} \quad \cot A = \frac{-3}{5}$$

$$\sec A = \frac{-\sqrt{34}}{3} \quad \csc A = \frac{\sqrt{34}}{5}$$

2. $\cos B = -\frac{5}{7}$ in Quadrant II. Find the other five exact trig values:

$$y = \sqrt{49 - 25} = \sqrt{24}$$

$$\sin B = \frac{\sqrt{24}}{7} \quad \cos B = -\frac{5}{7}$$

$$\tan B = \frac{-\sqrt{24}}{5} \quad \cot B = \frac{-5}{\sqrt{24}}$$

$$\sec B = -\frac{7}{5} \quad \csc B = \frac{7}{\sqrt{24}}$$

3. $\cot C = -\frac{60}{11}$ in Quadrant IV. Find the other five exact trig values:

$$x = 60, y = -11, r = 61$$

$$\sin C = \frac{-11}{61} \quad \cos C = \frac{60}{61}$$

$$\tan C = \frac{-11}{60} \quad \cot C = -\frac{60}{11}$$

$$\sec C = \frac{61}{60} \quad \csc C = -\frac{61}{11}$$

4. Find the approximate values of A, B, and C (in degrees) above.

$$A = \underline{120.964 \pm 360n}$$

$$B = \underline{135.585 \pm 360n}$$

$$C = \underline{-10.389 \pm 360n}$$

5. Find the approximate values of:

$$\cos -38^\circ = .788$$

$$\sin 46^\circ = .719$$

$$\tan 2.6 = -.602$$

$$\sec -.937 = 1.689$$

$$\csc 2.8 = 20.471$$

6. Find the approximate values (in degrees) of:

$$\cos^{-1} 1.725 = \left\{ \begin{array}{l} \text{No solution} \end{array} \right.$$

$$\sin^{-1} (-.345) = \left\{ \begin{array}{l} -20.182 \pm 360n \\ 200.182 \pm 360n \end{array} \right.$$

$$\tan^{-1} 1.788 = \left\{ \begin{array}{l} 60.782 \pm 360n \\ 240.782 \pm 360n \end{array} \right.$$

$$\sec^{-1} 2.082 = \left\{ \begin{array}{l} 61.295 \pm 360n \\ -61.295 \pm 360n \end{array} \right.$$

$$\csc^{-1} -1.362 = \left\{ \begin{array}{l} -47.241 \pm 360n \\ 227.241 \pm 360n \end{array} \right.$$

7. A boat sails 63 mph at a bearing of 113° . The current flows 8 mph at 254° . Find the magnitude and bearing of the resultant vector.

$$\vec{b} = 63 \cos 113^\circ \vec{i} + 63 \sin 113^\circ \vec{j}$$

$$\vec{c} = 8 \cos 254^\circ \vec{i} + 8 \sin 254^\circ \vec{j}$$

$$\vec{b} + \vec{c} = \cancel{55.526 \vec{i}} - \cancel{2.586 \vec{j}} = -26.821 \vec{i} + 50.302 \vec{j}$$

$$|\vec{b} + \vec{c}| = \cancel{55.623} = 57.066$$

$$\theta = \cos^{-1} \frac{55.623}{57.066} = \theta = \cos^{-1} \frac{-26.821}{57.066} = 118.066^\circ$$

8. If $\vec{s} = -4\vec{i} + 7\vec{j}$ and $\vec{r} = 15\vec{i} + 8\vec{j}$, find:

a. $4\vec{s} - 3\vec{r} =$

$$-16\vec{i} + 28\vec{j} - 45\vec{i} - 24\vec{j}$$

$$= -61\vec{i} + 4\vec{j}$$

b. $|3\vec{s} + 4\vec{r}| = |48\vec{i} + 53\vec{j}|$

$$= \sqrt{48^2 + 53^2} = \sqrt{5113}$$

$$\approx 71.505$$

c. The unit vector in the direction $\vec{r} = \frac{\vec{r}}{|\vec{r}|} = \frac{15}{17}\vec{i} + \frac{8}{17}\vec{j}$

9. Find the exact value of the following:

$$\sin \frac{3\pi}{4} \csc \frac{3\pi}{4} \tan \frac{5\pi}{6}$$

$$= \left(\frac{1}{\sqrt{2}}\right) \left(\frac{\sqrt{2}}{1}\right) \left(\frac{-1}{\sqrt{3}}\right)$$

$$= -\frac{1}{\sqrt{3}}$$

$$\frac{1}{\cos \frac{5\pi}{3} + \sin \frac{4\pi}{3}} + \frac{5}{\sin \frac{11\pi}{3} + \cos \frac{\pi}{3}}$$

$$= \frac{1}{\frac{1}{2} + \frac{\sqrt{3}}{2}} + \frac{1}{-\frac{\sqrt{3}}{2} + \frac{1}{2}}$$

$$= \frac{1}{\frac{1+\sqrt{3}}{2}} + \frac{1}{\frac{-\sqrt{3}+1}{2}} = \frac{2}{\sqrt{3}+1} + \frac{2}{1-\sqrt{3}}$$

$$= \frac{2(-\sqrt{3}+1) + 2(1+\sqrt{3})}{1-3} = \boxed{-2}$$