
DERIVATIVE OF A FUNCTION: $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ or $f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$

DIFFERENTIATION RULES:

(Where "u" and "v" are differentiable functions of x, and "a" is a constant.)

$$\frac{d}{dx} au = a \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(u + v) = \frac{du}{dx} + \frac{dv}{dx}$$

$$\frac{d}{dx} u^n = n u^{n-1} \cdot \frac{du}{dx}$$

$$\frac{d}{dx} a = 0$$

$$\frac{d}{dx}(uv) = u \cdot \frac{dv}{dx} + v \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \left(\frac{u}{v} \right) = \frac{v \cdot \frac{du}{dx} - u \cdot \frac{dv}{dx}}{v^2}$$

CHAIN RULE: $\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$

$$\frac{d}{dx} \sin u = \cos u \frac{du}{dx}$$

$$\frac{d}{dx} \cos u = -\sin u \frac{du}{dx}$$

$$\frac{d}{dx} \tan u = \sec^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \cot u = -\csc^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \sec u = \sec u \tan u \frac{du}{dx}$$

$$\frac{d}{dx} \csc u = -\csc u \cot u \frac{du}{dx}$$

$$\frac{d}{dx} \ln u = \frac{1}{u} \frac{du}{dx}$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\frac{d}{dx} a^u = a^u \ln a \frac{du}{dx}$$

$$\frac{d}{dx} \sin^{-1} u = \frac{\frac{du}{dx}}{\sqrt{1-u^2}}$$

$$\frac{d}{dx} \cos^{-1} u = \frac{-\frac{du}{dx}}{\sqrt{1-u^2}}$$

$$\frac{d}{dx} \tan^{-1} u = \frac{\frac{du}{dx}}{1+u^2}$$

$$\frac{d}{dx} \cot^{-1} u = \frac{-\frac{du}{dx}}{1+u^2}$$

$$\frac{d}{dx} \sec^{-1} u = \frac{\frac{du}{dx}}{|u|\sqrt{u^2-1}}$$

$$\frac{d}{dx} \csc^{-1} u = \frac{-\frac{du}{dx}}{|u|\sqrt{u^2-1}}$$