
DERIVATIVE OF A FUNCTION: $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ or $f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$

DIFFERENTIATION RULES:

(Where "u" and "v" are differentiable functions of x, and "a" is a constant.)

$$\frac{d}{dx} au = a \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(u + v) = \frac{du}{dx} + \frac{dv}{dx}$$

$$\frac{d}{dx} u^n = n u^{n-1} \cdot \frac{du}{dx}$$

$$\frac{d}{dx} a = 0$$

$$\frac{d}{dx}(uv) = u \cdot \frac{dv}{dx} + v \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \left(\frac{u}{v} \right) = \frac{v \cdot \frac{du}{dx} - u \cdot \frac{dv}{dx}}{v^2}$$

CHAIN RULE: $\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$

$$\frac{d}{dx} \sin u = \cos u \frac{du}{dx}$$

$$\frac{d}{dx} \cos u = -\sin u \frac{du}{dx}$$

$$\frac{d}{dx} \tan u = \sec^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \cot u = -\csc^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \sec u = \sec u \tan u \frac{du}{dx}$$

$$\frac{d}{dx} \csc u = -\csc u \cot u \frac{du}{dx}$$

$$\frac{d}{dx} \ln u = \frac{1}{u} \frac{du}{dx}$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\frac{d}{dx} a^u = a^u \ln a \frac{du}{dx}$$

$$\frac{d}{dx} \sin^{-1} u = \frac{\frac{du}{dx}}{\sqrt{1-u^2}}$$

$$\frac{d}{dx} \cos^{-1} u = \frac{-\frac{du}{dx}}{\sqrt{1-u^2}}$$

$$\frac{d}{dx} \tan^{-1} u = \frac{\frac{du}{dx}}{1+u^2}$$

$$\frac{d}{dx} \cot^{-1} u = \frac{-\frac{du}{dx}}{1+u^2}$$

$$\frac{d}{dx} \sec^{-1} u = \frac{\frac{du}{dx}}{|u|\sqrt{u^2-1}}$$

$$\frac{d}{dx} \csc^{-1} u = \frac{-\frac{du}{dx}}{|u|\sqrt{u^2-1}}$$

INTEGRATION FORMULAS:

$$\int f(x) dx = F(x) + C, \text{ where } F'(x) = f(x)$$

$$\frac{d}{dx} \int_a^x f(t) dt = f(x) \quad \text{[First Fundamental Theorem]}$$

Remember the Chain Rule!!!: $\frac{d}{dx} \int_a^u f(t) dt = f(u) \cdot D_x u$

$$\int_a^b f(x) dx = F(b) - F(a), \text{ where } F'(x) = f(x) \quad \text{[Second Fundamental Theorem]}$$

$$\int u^n du = \frac{u^{n+1}}{n+1} + C, n \neq -1$$

$$\int \frac{du}{u} = \ln |u| + C$$

$$\int e^u du = e^u + C$$

$$\int a^u du = \frac{a^u}{\ln a} + C, (a > 0, a \neq 1)$$

$$\int \sin u du = -\cos u + C$$

$$\int \cos u du = \sin u + C$$

$$\int \sec^2 u du = \tan u + C$$

$$\int \csc^2 u du = -\cot u + C$$

$$\int \sec u \cdot \tan u du = \sec u + C$$

$$\int \csc u \cdot \cot u du = -\csc u + C$$

$$\int \sec u du = \ln | \sec u + \tan u | + C$$

$$\int \tan u du = \ln | \sec u | + C$$

$$\int \csc u du = \ln | \csc u - \cot u | + C$$

$$\int \cot u du = \ln | \sin u | + C$$

$$\int \sin^2 u du = \frac{1}{2}u - \frac{1}{4}\sin 2u + C$$

$$\int \cos^2 u du = \frac{1}{2}u + \frac{1}{4}\sin 2u + C$$

$$\int \frac{du}{\sqrt{a^2 - u^2}} = \sin^{-1}\left(\frac{u}{a}\right) + C$$

$$\int \frac{du}{a^2 + u^2} = \frac{1}{a} \cdot \tan^{-1}\left(\frac{u}{a}\right) + C$$

$$\int \frac{du}{u\sqrt{u^2 - a^2}} = \frac{1}{a} \cdot \sec^{-1}\left|\frac{u}{a}\right| + C$$

$$\int \frac{du}{u^2 - a^2} = \frac{1}{2a} \ln \left(\frac{u-a}{u+a} \right) + C$$

$$\int u dv = uv - \int v du$$