

**Honors PreCalculus 2017-18**  
**PreCalc Basics Test**

**Name:** \_\_\_\_\_

**score** \_\_\_\_\_

1. If  $f(x)$  is a linear function  $f(3)=16$  and  $f(1)=10$ , then the equation of the line is

(a)  $f(x) = \frac{1}{3}x + 4$

(b)  $f(x) = 2x + 10$

(c)  $f(x) = \frac{1}{2}x + 4$

(d)  $f(x) = -\frac{1}{2}x + 10$

(e)  $f(x) = 3x + 7$

2. An equation for the line through the point  $(0, 4)$  and parallel to the line with the equation  $3x - y = 6$  is

(a)  $y = -3x + 4$

(b)  $y = 4x$

(c)  $y = 3x + 4$

(d)  $y = -\frac{1}{3}x + 4$

(e)  $y = 3x$

3. Find the vertex of the parabola  $-5x^2 - 40x + y - 78 = 0$ .

(a)  $(-4, 2)$

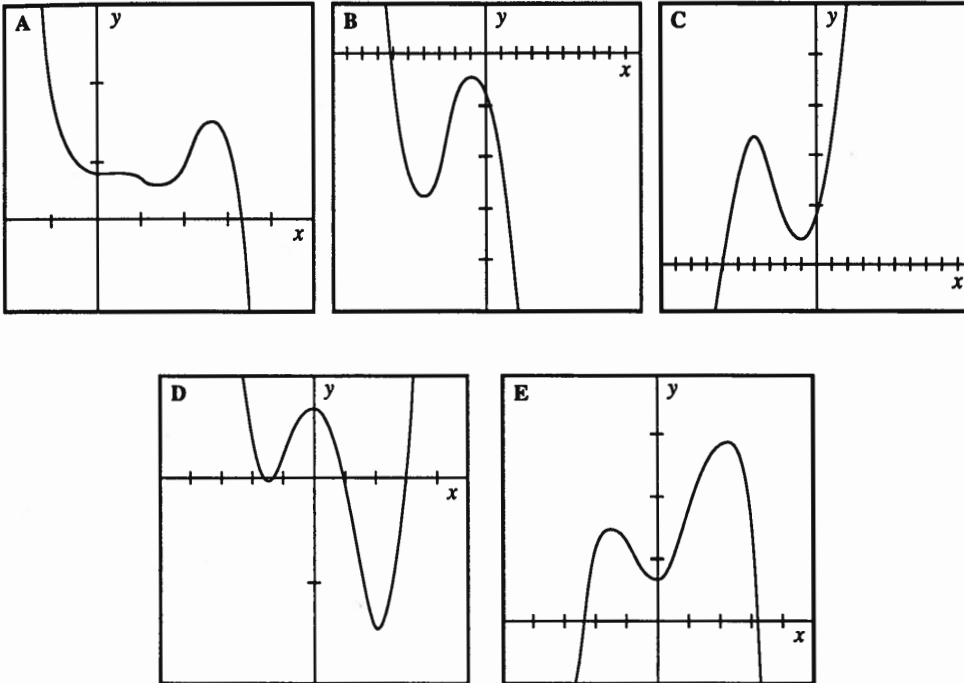
(b)  $(-2, -4)$

(c)  $(-4, -2)$

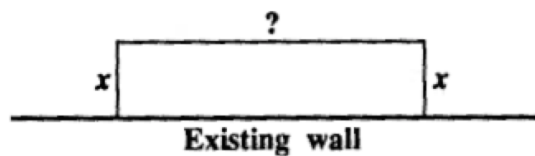
(d)  $(2, -4)$

(e)  $(4, 2)$

4. Which one of the following could represent a complete graph of  $f(x) = -x^3 + px^2 + qx + r$  where  $p, q,$  and  $r$  are real numbers?



5. Three sides of a fence and an existing wall form a rectangular enclosure. The *total* length of fence used is 180 feet. Let  $x$  be the length of the two sides perpendicular to the wall.



What possible  $x$ -values make sense in this problem?

- (a)  $x > 0$
- (b)  $0 < x < 180$
- (c)  $0 < x < 80$
- (d)  $x < 180$
- (e) None of these

6. Given this sign pattern  $f(x)$   $\leftarrow \begin{array}{cccc} - & 0 & + & 0 & - & 0 & - \\ & -4 & & -1 & & 2 & \end{array} \rightarrow$ , which of the following **might** be the equation of  $f(x)$ ?

- (a)  $f(x) = (x+4)(x+1)(x-2)$
- (b)  $f(x) = -(x+4)(x+1)(x-2)$
- (c)  $f(x) = -(x+4)(x+1)^2(x-2)$
- (d)  $f(x) = -(x+4)(x+1)^2(x-2)^2$
- (e)  $f(x) = -(x+4)^3(x+1)(x-2)^4$

7. Solve  $3x^2 - 5x < 2$ .

- (a)  $x < -\frac{1}{3}$  or  $2 < x$
- (b)  $-\frac{1}{3} < x < 2$
- (c)  $x < -2$  or  $\frac{1}{3} < x$
- (d)  $-2 < x < \frac{1}{3}$
- (e)  $-\frac{2}{3} < x < 1$

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**Round to 3 decimal places.**  
**Show all work.**

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1. Use your graphing calculator to find **and sketch** a complete graph of  $f(x) = x^4 - 21x^3 + 43x^2 - 14x - 8$ . State the window used, find the zeros, and the extreme points.

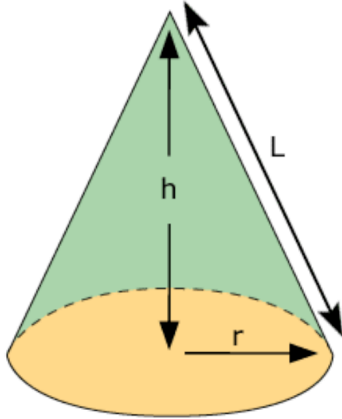
Window:

Zeros:

Extreme Points:

2. Find the zeros of  $y = -3x^4 - 19x^3 - 25x^2 + 19x + 28$  by calculator and prove it by synthetic division.

3. The volume of a right circular cone is given by  $V = \frac{1}{3}\pi r^2 h$  and the surface area is given by  $V = \pi r^2 + \pi r l$ . Given that  $r$ ,  $h$ , and  $l$  form a right triangle, what equation would you put in your calculator to find the radius which would determine the maximum volume of a cone with surface area =  $100\pi \text{ cm}^2$ ?



4. Use synthetic division to find  $f\left(-\frac{1}{2}\right)$  if  $f(x) = 8x^3 - 4x + 3$ .

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NO CALCULATOR ALLOWED  
Show all work.

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5. Find an inequality that has this sign pattern and solution:



$$x \in (-\infty, 0] \cup \{3\} \cup [4, \infty)$$

6. Show the sign patterns for  
 $y = -2x(3x - 5)^3(x - 5)^2$

$$y = (4 - x)^2(x + 3)(x + 1)$$

7. Show the sign pattern and solve  $-3x^4 - 19x^3 - 25x^2 + 19x + 28 < 0$ . (Note: This is the polynomial from #2 above)

8. Show the sign pattern and solve  $-9x^3 + 18x^2 + 4x - 8 > 0$