

Honors PreCalculus '20-21
Piece-Wise Defined Functions Test
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Calculator allowed

Name: _____

1.
$$f(x) = \begin{cases} \sqrt{-x^2 - 8x - 12}, & \text{if } -6 \leq x \leq -2 \\ x^2 - 4, & \text{if } -2 < x < 2 \\ \frac{2-x}{x}, & \text{if } 2 \leq x \end{cases}$$

i) Is $f(x)$ continuous at $x = -2$? Why or why not?

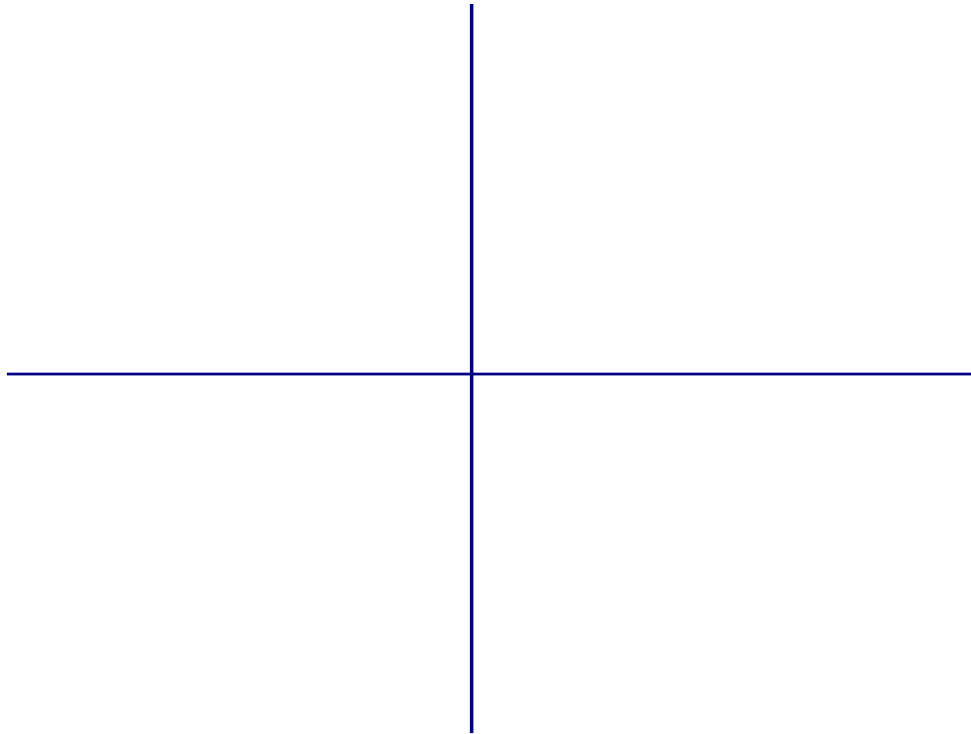
ii) Is $f(x)$ differentiable at $x = -2$? Why or why not?

$$2. \quad f(x) = \begin{cases} \sqrt{-x^2 - 8x - 12}, & \text{if } -6 \leq x \leq -2 \\ x^2 - 4, & \text{if } -2 < x < 2 \\ \frac{2-x}{x}, & \text{if } 2 \leq x \end{cases}$$

i) Is $f(x)$ continuous at $x = 2$? Why or why not?

ii) Is $f(x)$ differentiable at $x = 2$? Why or why not?

3. Sketch $f(x) = \begin{cases} \sqrt{-x^2 - 8x - 12}, & \text{if } -6 \leq x \leq -2 \\ x^2 - 4, & \text{if } -2 < x < 2 \\ \frac{2-x}{x}, & \text{if } 2 \leq x \end{cases}$. State the Traits listed.



Domain:

Range:

Zeros:

Y-int:

VAs:

EB (Left):

EB (Right):

x -values of discontinuities:

x -values of non-differentiability:

Extreme Points (provide non-graphical evidence):